

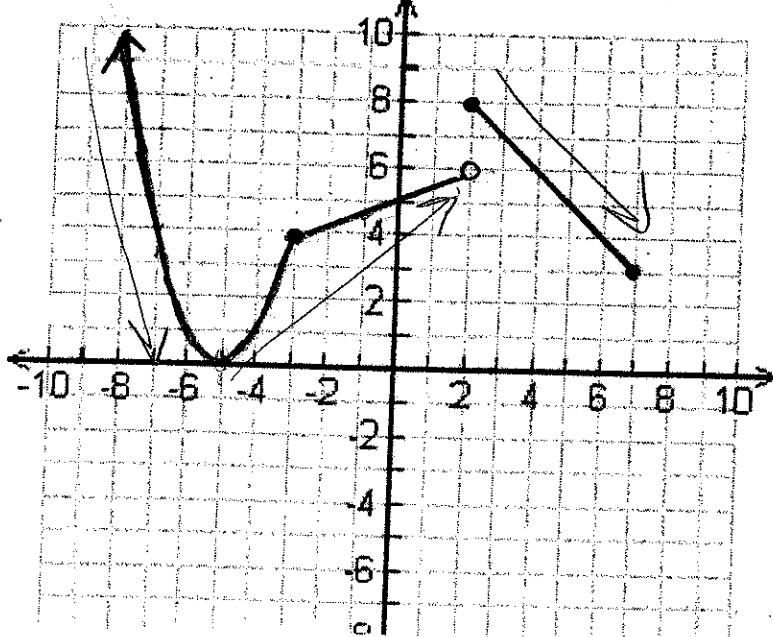
(Review)

AGS 2 Module 4

Name: Key Per: _____

LT 1: Communication LT 2: Patterns/Modeling LT 4: Solving	LT 1	LT 2	LT 4
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1. Use the graph below to answer the following questions.



a. Maximum None

b. Minimum (-5, 0)

c. Interval(s) where Increasing [-5, 2]

d. Interval(s) where Decreasing (-\infty; -5] \cup [2, 7]

e. Domain (-\infty, 7]

X-values

Y-values

f. Range [0, \infty)

g. x-intercept(s): (-5, 0)

h. y-intercept(s): (0, 5)

i. $f(-1) + f(2) = 4.5 + 8 = 12.5$

j. When $f(x) = 4$, Find $x = -7, -3, 6$

k. Continuous or Discontinuous? Why?

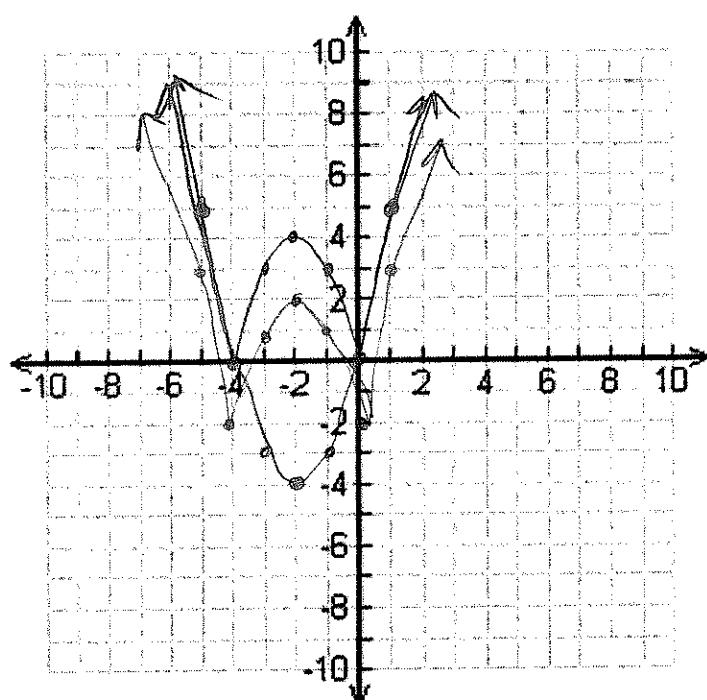
Need TO PICK up Pencil!

2. Graph each function on the same graph below:

a. $f(x) = (x+2)^2 - 4 \downarrow (-2, -4)$

b. $g(x) = |(x+2)^2 - 4|$

c. $h(x) = |(x+2)^2 - 4| - 2 \downarrow$



d. Write the piecewise function for $h(x)$

$$f(x) = \begin{cases} ((x+2)^2 - 4) - 2 & x \leq -4 \text{ and } x \geq 0 \\ -((x+2)^2 - 4) - 2 & -4 < x < 0 \end{cases}$$

X	Y
-5	5
-4	0
-3	-3
-2	-4
-1	-3
0	0
1	5

X	Y
-5	5
-4	0
-3	3
-2	4
-1	3
0	0
1	5

3. Using the function $f(x) = |x - 3| + 5$ for the following problems:

a. $f(4) = 6$ $f(4) = 4 - 3 + 5 \rightarrow f(4) = 1 + 5$
 $f(4) = 11 + 5 \rightarrow f(4) = 6$

b. $f(-5) = 13$ $f(-5) = |-5 - 3| + 5 \rightarrow f(-5) = 8 + 5$
 $f(-5) = |-8| + 5 \rightarrow f(-5) = 13$

c. $f(x) = 1$, $x = \underline{\hspace{2cm}}$ and $x = \underline{\hspace{2cm}}$ Not possible

$$1 = |x - 3| + 5$$

$$-4 = |x - 3| \leftarrow \begin{array}{l} \text{Absolute value cannot be equal} \\ \text{to something negative} \end{array}$$

d. $f(x) = 7$, $x = \underline{\hspace{2cm}}$ and $x = \underline{\hspace{2cm}}$

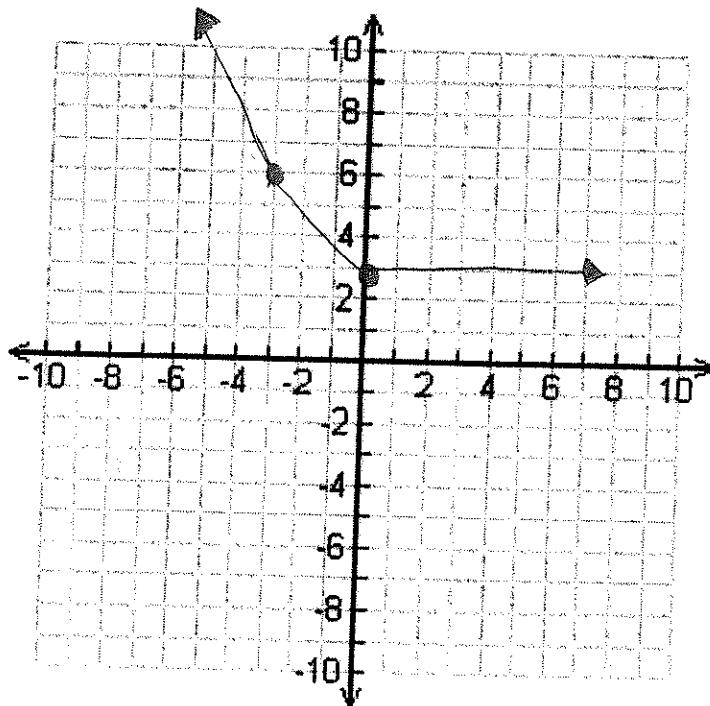
$$7 = |x - 3| + 5$$

$$2 = |x - 3| \rightarrow \begin{array}{l} 2 = x - 3 \\ 5 = x \end{array}$$

$$-2 = x - 3 \rightarrow \begin{array}{l} -2 = x \\ 1 = x \end{array}$$

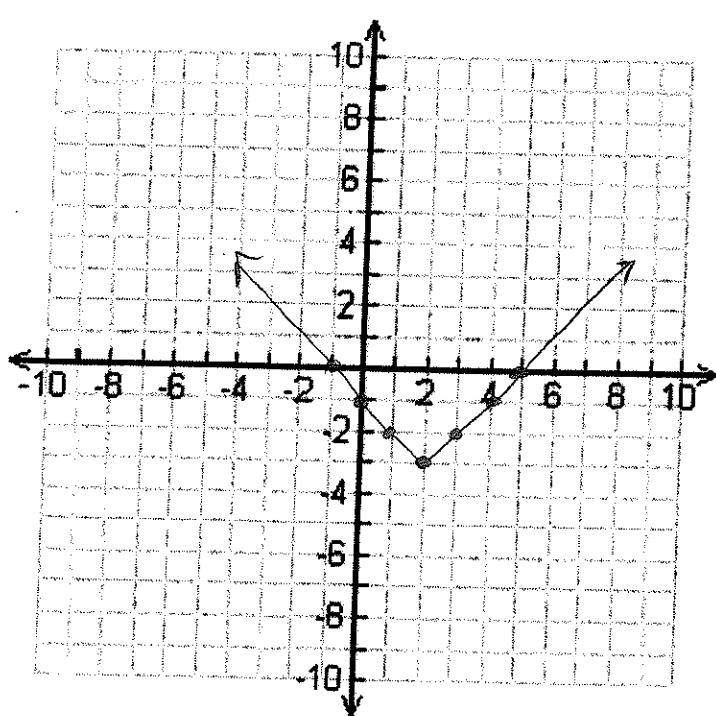
3. Graph the piecewise function:

$$f(x) = \begin{cases} -2x & x \leq -3 \\ -x + 3 & -3 < x < 0 \\ 3 & x \geq 0 \end{cases}$$



4. Graph the following function and give the piecewise function

$$f(x) = |x - 2| - 3$$



Piecewise Function:

$$f(x) = \begin{cases} (x-2) - 3 & x \geq 2 \\ -(x-2) - 3 & x < 2 \end{cases}$$

a. $f(2) = -3$

b. $f(6) = 1$

5. Show the inverses to the following function through equations, tables, and graphs. Please label your graphs showing which is the original function and which is the inverse:

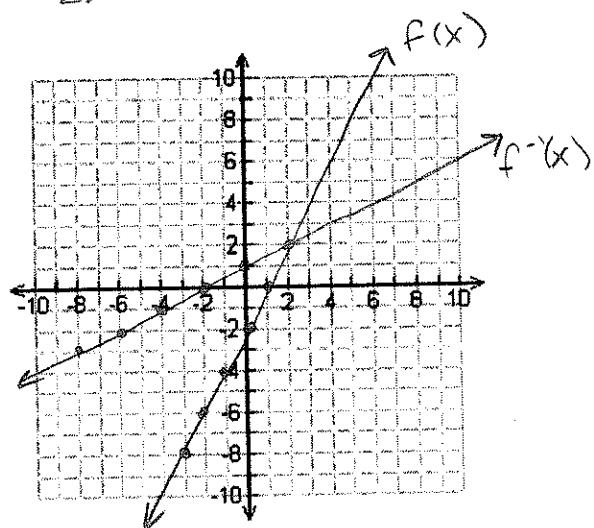
a. $f(x) = 2x - 2$

x	$f(x)$
-3	-8
-2	-6
-1	-4
0	-2
1	0
2	2
3	4

x	$f^{-1}(x)$
-8	-3
-6	-2
-4	-1
-2	0
0	1
2	2
4	3

Inverse: $f^{-1}(x) = \frac{x+2}{2}$ or $\frac{1}{2}x + 1$

$$\begin{aligned} y &= 2x - 2 \\ x &= 2y - 2 \\ x + 2 &= 2y \\ y &= \frac{x+2}{2} \\ y &= \frac{1}{2}x + 1 \end{aligned}$$



6. Solve each function to find its inverse.

a. $g(x) = x^2 + 4$ $x = y^2 + 4$ $\sqrt{x-4} = \sqrt{y^2}$ $\sqrt{x-4} = y$ Inverse: $g^{-1}(x) = \sqrt{x-4}$

b. $h(x) = -3x - 6$ $x = -3y - 6$ $\frac{x+6}{-3} = y$ Inverse: $h^{-1}(x) = \frac{x+6}{-3}$ or $-\frac{1}{3}x - 2$

c. $j(x) = \frac{1}{2}x + 8$ $x = \frac{1}{2}y + 8$ $2(x-8) = (\frac{1}{2}y)^2$ $2x - 16 = y$ Inverse: $j^{-1}(x) = 2x - 16$

d. $p(x) = (1, 2), (3, -1), (9, 7), (-6, 5), (4, \frac{1}{2})$
Inverse: $p^{-1}(x) = (2, 1), (-1, 3), (7, 9), (5, -6), (\frac{1}{2}, 4)$